



Quality by Design approach in the development of hydrophilic interaction liquid chromatographic method for the analysis of iohexol and its impurities

The objective of this research paper is to develop a hydrophilic interaction liquid chromatographic method for the analysis of iohexol, its endo-isomer and three impurities following Quality by Design approach. Design of experiments (DoE) methodology is implemented for the creation of the relationship between critical process parameters and critical quality attributes.

The factors (independent variables) examined are: X_1 = acetonitrile content in the mobile phase (%), X_2 = pH of the water phase and X_3 = ammonium acetate concentration in the water phase (mmol/L). All the factors are continuous. The responses (dependent variables) examined are: k_1 = retention time of related compound C, k_2 = retention time of related compound B, k_3 = retention time of related compound A, k_4 = retention time of exo-iohexol and k_5 = retention time of endo-iohexol. The applied DoE method is Box Behnken design.

Isalos version used: 2.0.6

Scientific article: <https://www.sciencedirect.com/science/article/abs/pii/S073170851500151X>

Step 1: Box Behnken Design

In the first tab named “Action” define the factors in the column headers and fill each column with the low and high levels of the corresponding factors. This tab can be renamed “Box Behnken”. Afterwards, apply the Box Behnken method: DOE → Response Surface → Box Behnken

| | Col1 | Col2 (I) | Col3 (I) | Col4 (I) |
|-------------|-------------|----------|----------|----------|
| User Header | User Row ID | X1 | X2 | X3 |
| 1 | | 80 | 3 | 20 |
| 2 | | 90 | 7 | 80 |

DoE Box Behnken

Number of Center Points per Block: 3

Number of Replicates: 1

Number of Blocks: 1

Random Standard order

Excluded Columns

Included Columns

Col2 -- X1
Col3 -- X2
Col4 -- X3

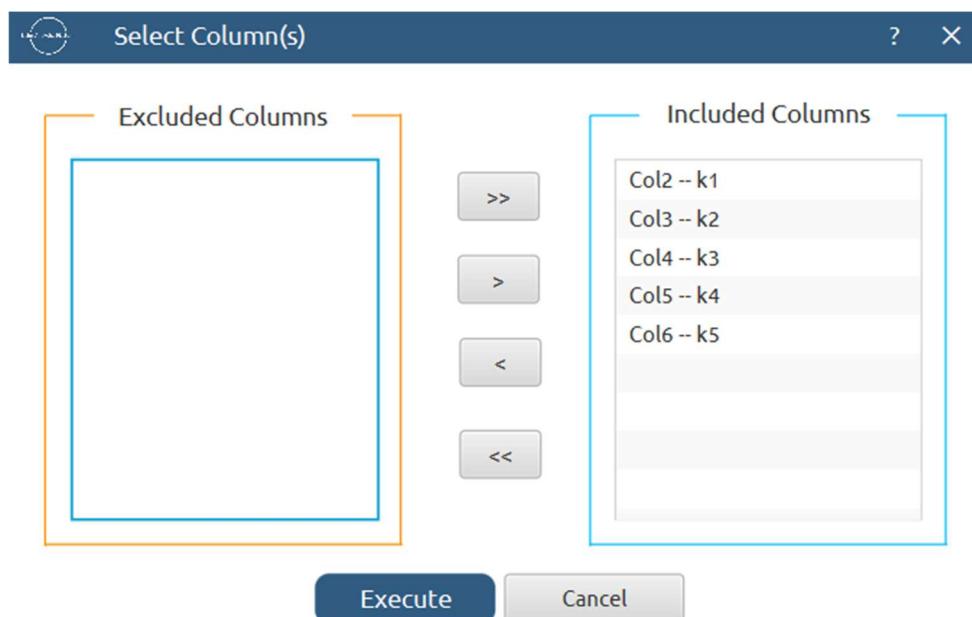
Results (right spreadsheet):

| | Col1 | Col2 (I) | Col3 (S) | Col4 (S) | Col5 (S) | Col6 (D) | Col7 (D) | Col8 (D) |
|-------------|-------------|----------------|--------------|------------------|--------------|----------|----------|----------|
| User Header | User Row ID | Standard Order | Block Number | Replicate Number | Point Type | X1 | X2 | X3 |
| 1 | | 1 | Block: 1 | Replicate: 1 | Design Point | 80.0 | 3.0 | 50.0 |
| 2 | | 2 | Block: 1 | Replicate: 1 | Design Point | 90.0 | 3.0 | 50.0 |
| 3 | | 3 | Block: 1 | Replicate: 1 | Design Point | 80.0 | 7.0 | 50.0 |
| 4 | | 4 | Block: 1 | Replicate: 1 | Design Point | 90.0 | 7.0 | 50.0 |
| 5 | | 5 | Block: 1 | Replicate: 1 | Design Point | 80.0 | 5.0 | 20.0 |
| 6 | | 6 | Block: 1 | Replicate: 1 | Design Point | 90.0 | 5.0 | 20.0 |
| 7 | | 7 | Block: 1 | Replicate: 1 | Design Point | 80.0 | 5.0 | 80.0 |
| 8 | | 8 | Block: 1 | Replicate: 1 | Design Point | 90.0 | 5.0 | 80.0 |
| 9 | | 9 | Block: 1 | Replicate: 1 | Design Point | 85.0 | 3.0 | 20.0 |
| 10 | | 10 | Block: 1 | Replicate: 1 | Design Point | 85.0 | 7.0 | 20.0 |
| 11 | | 11 | Block: 1 | Replicate: 1 | Design Point | 85.0 | 3.0 | 80.0 |
| 12 | | 12 | Block: 1 | Replicate: 1 | Design Point | 85.0 | 7.0 | 80.0 |
| 13 | | 13 | Block: 1 | ---- | Center Point | 85.0 | 5.0 | 50.0 |
| 14 | | 14 | Block: 1 | ---- | Center Point | 85.0 | 5.0 | 50.0 |
| 15 | | 15 | Block: 1 | ---- | Center Point | 85.0 | 5.0 | 50.0 |

Step 2: Definition of response variables

Create a new tab named “Responses” and define the responses in the column headers. Fill each column with the values of the corresponding responses that were observed and make sure the values follow the order of the experiments as given by the Box Behnken method. Then, select all columns to be transferred to the right spreadsheet: *Data Transformation → Data Manipulation → Select Column(s)*

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) | Col6 (D) |
|-------------|-------------|----------|----------|----------|----------|----------|
| User Header | User Row ID | k1 | k2 | k3 | k4 | k5 |
| 1 | | 0.11 | 0.41 | 0.71 | 1.11 | 1.39 |
| 2 | | 1.45 | 3.28 | 6.16 | 12.04 | 15.31 |
| 3 | | 0.1 | 0.38 | 0.66 | 1.03 | 1.29 |
| 4 | | 1.3 | 2.86 | 5.41 | 10.31 | 13.13 |
| 5 | | 0.08 | 0.35 | 0.61 | 0.96 | 1.2 |
| 6 | | 1.26 | 2.8 | 5.2 | 9.95 | 12.51 |
| 7 | | 0.11 | 0.4 | 0.71 | 1.12 | 1.4 |
| 8 | | 1.35 | 2.9 | 5.62 | 10.66 | 13.73 |
| 9 | | 0.36 | 0.93 | 1.58 | 2.63 | 3.27 |
| 10 | | 0.37 | 0.89 | 1.53 | 2.55 | 3.17 |
| 11 | | 0.44 | 1.04 | 1.83 | 3.05 | 3.84 |
| 12 | | 0.42 | 0.96 | 1.7 | 2.81 | 3.53 |
| 13 | | 0.38 | 0.92 | 1.61 | 2.66 | 3.34 |
| 14 | | 0.39 | 0.91 | 1.61 | 2.67 | 3.35 |
| 15 | | 0.4 | 0.92 | 1.62 | 2.68 | 3.18 |



Step 3: Data isolation

Create a new tab named “Data” and import the results from the “Box Behnken” and “Responses” spreadsheets by right clicking on the left spreadsheet. Then, select only the factors and responses columns to be transferred to the right spreadsheet: *Data Transformation* → *Data Manipulation* → *Select Column(s)*

| | Col1 | Col2 | Col3 | Col4 | Col5 | Col6 | |
|-------------|-------------|------|------|------|------|------|--|
| User Header | User Row ID | | | | | | |
| 1 | | | | | | | |
| 2 | | | | | | | |
| 3 | | | | | | | |
| 4 | | | | | | | |
| 5 | | | | | | | |
| 6 | | | | | | | |
| 7 | | | | | | | |
| 8 | | | | | | | |
| 9 | | | | | | | |
| 10 | | | | | | | |

Join Configuration Steps

Step 1: Box Behnken & Responses (Concatenation)

Join Type

Concatenation Left Join Right Join Inner Join Full Outer Join

Left Spreadsheet: Box Behnken Right Spreadsheet: Responses

Join Column

Common header name Different header names

Add Delete Execute Cancel

Excluded Columns

Col2 -- Standard Order
Col3 -- Block Number
Col4 -- Replicate Number
Col5 -- Point Type

Included Columns

Col6 -- X1
Col7 -- X2
Col8 -- X3
Col9 -- k1
Col10 -- k2
Col11 -- k3
Col12 -- k4
Col13 -- k5

>>
>
<
<<

Execute Cancel

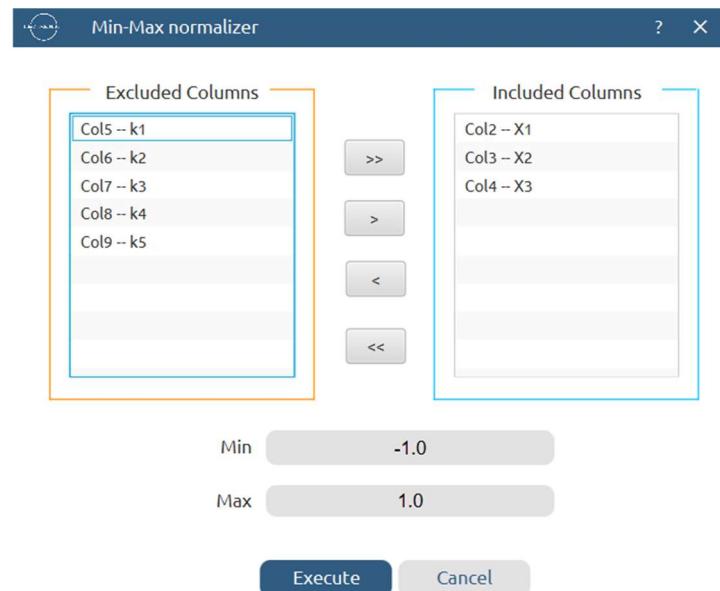
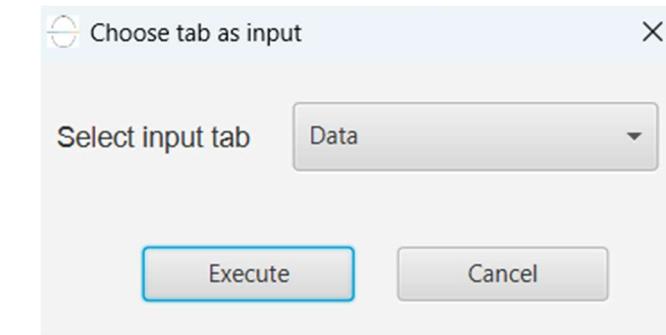
Results:

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) | Col8 (D) | Col9 (D) |
|-------------|-------------|----------|----------|----------|----------|----------|----------|----------|----------|
| User Header | User Row ID | X1 | X2 | X3 | k1 | k2 | k3 | k4 | k5 |
| 1 | | 80.0 | 3.0 | 50.0 | 0.11 | 0.41 | 0.71 | 1.11 | 1.39 |
| 2 | | 90.0 | 3.0 | 50.0 | 1.45 | 3.28 | 6.16 | 12.04 | 15.31 |
| 3 | | 80.0 | 7.0 | 50.0 | 0.1 | 0.38 | 0.66 | 1.03 | 1.29 |
| 4 | | 90.0 | 7.0 | 50.0 | 1.3 | 2.86 | 5.41 | 10.31 | 13.13 |
| 5 | | 80.0 | 5.0 | 20.0 | 0.08 | 0.35 | 0.61 | 0.96 | 1.2 |
| 6 | | 90.0 | 5.0 | 20.0 | 1.26 | 2.8 | 5.2 | 9.95 | 12.51 |
| 7 | | 80.0 | 5.0 | 80.0 | 0.11 | 0.4 | 0.71 | 1.12 | 1.4 |
| 8 | | 90.0 | 5.0 | 80.0 | 1.35 | 2.9 | 5.62 | 10.66 | 13.73 |
| 9 | | 85.0 | 3.0 | 20.0 | 0.36 | 0.93 | 1.58 | 2.63 | 3.27 |
| 10 | | 85.0 | 7.0 | 20.0 | 0.37 | 0.89 | 1.53 | 2.55 | 3.17 |
| 11 | | 85.0 | 3.0 | 80.0 | 0.44 | 1.04 | 1.83 | 3.05 | 3.84 |
| 12 | | 85.0 | 7.0 | 80.0 | 0.42 | 0.96 | 1.7 | 2.81 | 3.53 |
| 13 | | 85.0 | 5.0 | 50.0 | 0.38 | 0.92 | 1.61 | 2.66 | 3.34 |
| 14 | | 85.0 | 5.0 | 50.0 | 0.39 | 0.91 | 1.61 | 2.67 | 3.35 |
| 15 | | 85.0 | 5.0 | 50.0 | 0.4 | 0.92 | 1.62 | 2.68 | 3.18 |

Step 4: Normalization

Create a new tab named “Normalized data” and import the results from the “Data” spreadsheet. Afterwards, normalize the factor columns to take values in the range [-1, 1]: [Data Transformation → Normalizers → Min-Max](#)

| | Col1 | Col2 | Col3 | Col4 | Col5 | Col6 | |
|-------------|-------------|------|------|------|------|------|-----------------------------------|
| User Header | User Row ID | | | | | | |
| 1 | | | | | | | |
| 2 | | | | | | | |
| 3 | | | | | | | Import from File |
| 4 | | | | | | | Import from Spreadsheet |
| 5 | | | | | | | Import from Multiple Spreadsheets |
| 6 | | | | | | | Adjust Spreadsheet Precision |
| 7 | | | | | | | Export Spreadsheet Data |
| 8 | | | | | | | Clear Spreadsheet |
| 9 | | | | | | | |
| 10 | | | | | | | |



Results:

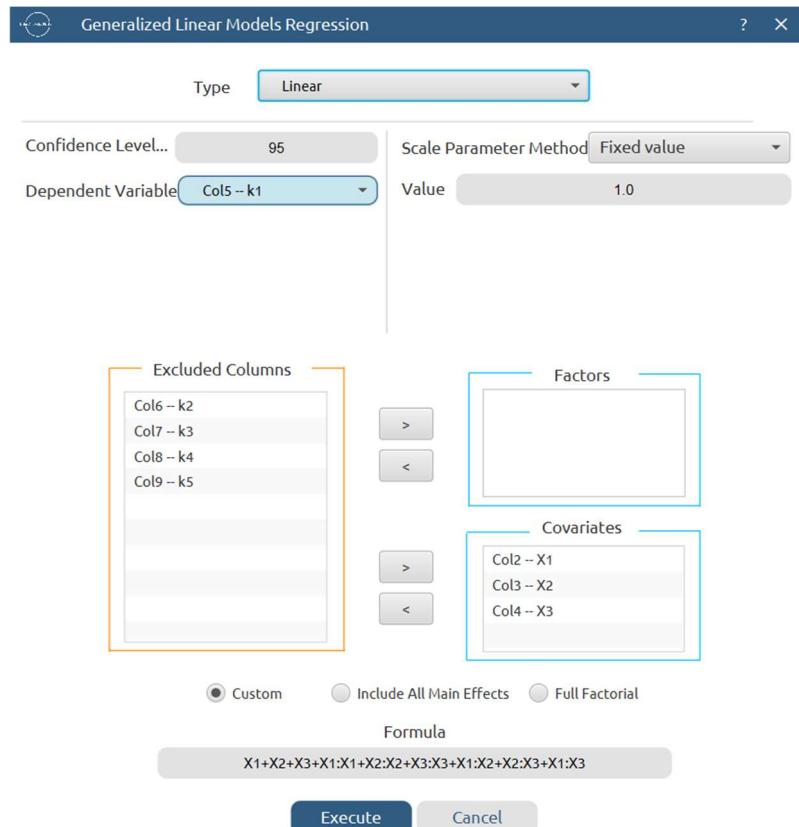
| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) | Col8 (D) | Col9 (D) |
|-------------|-------------|----------|----------|----------|----------|----------|----------|----------|----------|
| User Header | User Row ID | X1 | X2 | X3 | k1 | k2 | k3 | k4 | k5 |
| 1 | | -1.0 | -1.0 | 0.0 | 0.11 | 0.41 | 0.71 | 1.11 | 1.39 |
| 2 | | 1.0 | -1.0 | 0.0 | 1.45 | 3.28 | 6.16 | 12.04 | 15.31 |
| 3 | | -1.0 | 1.0 | 0.0 | 0.1 | 0.38 | 0.66 | 1.03 | 1.29 |
| 4 | | 1.0 | 1.0 | 0.0 | 1.3 | 2.86 | 5.41 | 10.31 | 13.13 |
| 5 | | -1.0 | 0.0 | -1.0 | 0.08 | 0.35 | 0.61 | 0.96 | 1.2 |
| 6 | | 1.0 | 0.0 | -1.0 | 1.26 | 2.8 | 5.2 | 9.95 | 12.51 |
| 7 | | -1.0 | 0.0 | 1.0 | 0.11 | 0.4 | 0.71 | 1.12 | 1.4 |
| 8 | | 1.0 | 0.0 | 1.0 | 1.35 | 2.9 | 5.62 | 10.66 | 13.73 |
| 9 | | 0.0 | -1.0 | -1.0 | 0.36 | 0.93 | 1.58 | 2.63 | 3.27 |
| 10 | | 0.0 | 1.0 | -1.0 | 0.37 | 0.89 | 1.53 | 2.55 | 3.17 |
| 11 | | 0.0 | -1.0 | 1.0 | 0.44 | 1.04 | 1.83 | 3.05 | 3.84 |
| 12 | | 0.0 | 1.0 | 1.0 | 0.42 | 0.96 | 1.7 | 2.81 | 3.53 |
| 13 | | 0.0 | 0.0 | 0.0 | 0.38 | 0.92 | 1.61 | 2.66 | 3.34 |
| 14 | | 0.0 | 0.0 | 0.0 | 0.39 | 0.91 | 1.61 | 2.67 | 3.35 |
| 15 | | 0.0 | 0.0 | 0.0 | 0.4 | 0.92 | 1.62 | 2.68 | 3.18 |

Step 5: Regression

The goal here is to produce a regression equation that includes main effects, two-factor interactions and quadratic effects for k_1 :

$$k = b_0 + b_1X_1 + b_2X_2 + b_3X_3 + b_{12}X_1X_2 + b_{13}X_1X_3 + b_{23}X_2X_3 + b_{11}X_1^2 + b_{22}X_2^2 + b_{33}X_3^2$$

Create a new tab named “Regression – k1” and import the results from the spreadsheet “Normalized data”. Afterwards, fit a generalized linear model to the data: Analytics → Regression → Statistical fitting → Generalized Linear Models



Results:

| k1 | Prediction |
|------|------------|
| 0.11 | 0.1062500 |
| 1.45 | 1.41625 |
| 0.1 | 0.1337500 |
| 1.3 | 1.3037500 |
| 0.08 | 0.0637500 |
| | |
| 1.26 | 1.27375 |
| 0.11 | 0.0962500 |
| | |
| 1.35 | 1.3662500 |
| | |
| 0.36 | 0.3800000 |
| | |
| 0.37 | 0.3525000 |
| | |
| 0.44 | 0.4575000 |
| | |
| 0.42 | 0.4000000 |
| | |
| 0.38 | 0.39 |
| | |
| 0.39 | 0.39 |
| | |
| 0.4 | 0.39 |

| Goodness of Fit | |
|--------------------------------------|-------------|
| | Value |
| Deviance | 0.0048250 |
| Scaled Deviance | 0.0048250 |
| Pearson Chi-Square | 0.0048250 |
| Scaled Pearson Chi-Square | 0.0048250 |
| Log Likelihood | -13.7864905 |
| Akaike's Information Criterion (AIC) | 47.5729810 |
| Finite Sample Corrected AIC (AIACC) | 102.5729810 |
| Bayesian Information Criterion (BIC) | 54.6534830 |
| Consistent AIC #(CAIC) | 64.6534830 |

| Parameter Estimates | | | | | | | |
|---------------------|-------------|------------|------------|-----------|----------------|----|-----------|
| Variable | Coefficient | Std. Error | Lower CI | Upper CI | Test Statistic | df | p-value |
| intercept | 0.39 | 0.5773503 | -0.7415857 | 1.5215857 | 0.4563000 | 1 | 0.4993583 |
| X1 | 0.62 | 0.3535534 | -0.0729519 | 1.3129519 | 3.0752000 | 1 | 0.0794948 |
| X2 | -0.0212500 | 0.3535534 | -0.7142019 | 0.6717019 | 0.0036125 | 1 | 0.9520727 |
| X3 | 0.0312500 | 0.3535534 | -0.6617019 | 0.7242019 | 0.0078125 | 1 | 0.9295680 |
| X1*X3 | 0.0150000 | 0.5 | -0.9649820 | 0.9949820 | 0.0009000 | 1 | 0.9760671 |
| X1*X2 | -0.0350000 | 0.5 | -1.0149820 | 0.9449820 | 0.0049000 | 1 | 0.9441937 |
| X2*X3 | -0.0075000 | 0.5 | -0.9874820 | 0.9724820 | 0.0002250 | 1 | 0.9880322 |
| X1*X1 | 0.3262500 | 0.5204165 | -0.6937476 | 1.3462476 | 0.3930058 | 1 | 0.5307237 |
| X2*X2 | 0.02375 | 0.5204165 | -0.9962476 | 1.0437476 | 0.0020827 | 1 | 0.9636000 |
| X3*X3 | -0.0162500 | 0.5204165 | -1.0362476 | 1.0037476 | 0.0009750 | 1 | 0.9750901 |

Repeat this step for the rest of the response variables. Results, k_2 :

| k_2 | Prediction |
|-------|------------|
| 0.41 | 0.4187500 |
| 3.28 | 3.1887500 |
| 0.38 | 0.4712500 |
| 2.86 | 2.8512500 |
| 0.35 | 0.2962500 |
| | |
| 2.8 | 2.8462500 |
| 0.4 | 0.3537500 |
| 2.9 | 2.9537500 |
| 0.93 | 0.9750000 |
| 0.89 | 0.8525000 |
| 1.04 | 1.0775000 |
| 0.96 | 0.9150000 |
| 0.92 | 0.9166667 |
| 0.91 | 0.9166667 |
| 0.92 | 0.9166667 |

| | |
|--------------------------------------|-------------|
| Goodness of Fit | |
| | Value |
| Deviance | 0.0337917 |
| Scaled Deviance | 0.0337917 |
| Pearson Chi-Square | 0.0337917 |
| Scaled Pearson Chi-Square | 0.0337917 |
| Log Likelihood | -13.8009738 |
| Akaike's Information Criterion (AIC) | 47.6019477 |
| Finite Sample Corrected AIC (AICC) | 102.6019477 |
| Bayesian Information Criterion (BIC) | 54.6824497 |
| Consistent AIC (CAIC) | 64.6824497 |

| Parameter Estimates | | | | | | | |
|---------------------|-------------|------------|------------|-----------|----------------|----|-----------|
| Variable | Coefficient | Std. Error | Lower CI | Upper CI | Test Statistic | df | p-value |
| intercept | 0.9166667 | 0.5773503 | -0.2149191 | 2.0482524 | 2.5208333 | 1 | 0.1123512 |
| X1 | 1.2875000 | 0.3535534 | 0.5945481 | 1.9804519 | 13.2612500 | 1 | 0.0002709 |
| X2 | -0.0712500 | 0.3535534 | -0.7642019 | 0.6217019 | 0.0406125 | 1 | 0.8402877 |
| X3 | 0.0412500 | 0.3535534 | -0.6517019 | 0.7342019 | 0.0136125 | 1 | 0.9071195 |
| X1*X3 | 0.0125000 | 0.5 | -0.9674820 | 0.9924820 | 0.0006250 | 1 | 0.9800550 |
| X1*X2 | -0.0975000 | 0.5 | -1.0774820 | 0.8824820 | 0.0380250 | 1 | 0.8453929 |
| X2*X3 | -0.0100000 | 0.5 | -0.9899820 | 0.9699820 | 0.0004000 | 1 | 0.9840434 |
| X1*X1 | 0.7366667 | 0.5204165 | -0.2833309 | 1.7566643 | 2.0037333 | 1 | 0.1569123 |
| X2*X2 | 0.0791667 | 0.5204165 | -0.9408309 | 1.0991643 | 0.0231410 | 1 | 0.8790909 |
| X3*X3 | -0.0408333 | 0.5204165 | -1.0608309 | 0.9791643 | 0.0061564 | 1 | 0.9374599 |

Results, k₃:

| k3 | Prediction |
|------|------------|
| 0.71 | 0.7200000 |
| 6.16 | 5.9950000 |
| 0.66 | 0.8250000 |
| 5.41 | 5.4 |
| 0.61 | 0.5350000 |
| 5.2 | 5.3000000 |
| 0.71 | 0.6100000 |
| 5.62 | 5.695 |
| 1.58 | 1.645 |
| 1.53 | 1.4400000 |
| 1.83 | 1.9200000 |
| 1.7 | 1.6350000 |
| 1.61 | 1.6133333 |
| 1.61 | 1.6133333 |
| 1.62 | 1.6133333 |

| | |
|--------------------------------------|-------------|
| Goodness of Fit | |
| Value | |
| Deviance | 0.1106167 |
| Scaled Deviance | 0.1106167 |
| Pearson Chi-Square | 0.1106167 |
| Scaled Pearson Chi-Square | 0.1106167 |
| Log Likelihood | -13.8393863 |
| Akaike's Information Criterion (AIC) | 47.6787727 |
| Finite Sample Corrected AIC (AICC) | 102.6787727 |
| Bayesian Information Criterion (BIC) | 54.7592747 |
| Consistent AIC (CAIC) | 64.7592747 |

| Parameter Estimates | | | | | | | |
|---------------------|-------------|------------|------------|-----------|----------------|----|-----------|
| Variable | Coefficient | Std. Error | Lower CI | Upper CI | Test Statistic | df | p-value |
| intercept | 1.6133333 | 0.5773503 | 0.4817476 | 2.7449191 | 7.8085333 | 1 | 0.0052000 |
| X1 | 2.4625000 | 0.3535534 | 1.7695481 | 3.1554519 | 48.5112500 | 1 | 0E-7 |
| X2 | -0.1225000 | 0.3535534 | -0.8154519 | 0.5704519 | 0.1200500 | 1 | 0.7289803 |
| X3 | 0.1175000 | 0.3535534 | -0.5754519 | 0.8104519 | 0.1104500 | 1 | 0.7396324 |
| X1*X3 | 0.0800000 | 0.5 | -0.8999820 | 1.0599820 | 0.0256000 | 1 | 0.8728811 |
| X1*X2 | -0.1750000 | 0.5 | -1.1549820 | 0.8049820 | 0.1225000 | 1 | 0.7263387 |
| X2*X3 | -0.0200000 | 0.5 | -0.9999820 | 0.9599820 | 0.0016000 | 1 | 0.9680931 |
| X1*X1 | 1.4983333 | 0.5204165 | 0.4783357 | 2.5183309 | 8.2892410 | 1 | 0.0039881 |
| X2*X2 | 0.1233333 | 0.5204165 | -0.8966643 | 1.1433309 | 0.0561641 | 1 | 0.8126648 |
| X3*X3 | -0.0766667 | 0.5204165 | -1.0966643 | 0.9433309 | 0.0217026 | 1 | 0.8828811 |

Results, k4:

| k4 | Prediction |
|-------|------------|
| 1.11 | 1.1337500 |
| 12.04 | 11.64375 |
| 1.03 | 1.4262500 |
| 10.31 | 10.2862500 |
| 0.96 | 0.7737500 |
| 9.95 | 10.1837500 |
| 1.12 | 0.8862500 |
| 10.66 | 10.8462500 |
| 2.63 | 2.7925000 |
| 2.55 | 2.3400000 |
| 3.05 | 3.2600000 |
| 2.81 | 2.6475000 |
| 2.66 | 2.6700000 |
| 2.67 | 2.6700000 |
| 2.68 | 2.6700000 |

| | |
|--------------------------------------|-------------|
| Goodness of Fit | |
| | Value |
| Deviance | 0.6350250 |
| Scaled Deviance | 0.6350250 |
| Pearson Chi-Square | 0.6350250 |
| Scaled Pearson Chi-Square | 0.6350250 |
| Log Likelihood | -14.1015905 |
| Akaike's Information Criterion (AIC) | 48.2031810 |
| Finite Sample Corrected AIC (AICC) | 103.2031810 |
| Bayesian Information Criterion (BIC) | 55.2836830 |
| Consistent AIC (CAIC) | 65.2836830 |

| Parameter Estimates | | | | | | | |
|---------------------|-------------|------------|------------|-----------|----------------|----|-----------|
| Variable | Coefficient | Std. Error | Lower CI | Upper CI | Test Statistic | df | p-value |
| intercept | 2.6700000 | 0.5773503 | 1.5384143 | 3.8015857 | 21.3867000 | 1 | 0.0000038 |
| X1 | 4.8425000 | 0.3535534 | 4.1495481 | 5.5354519 | 187.5984500 | 1 | 0.0 |
| X2 | -0.2662500 | 0.3535534 | -0.9592019 | 0.4267019 | 0.5671125 | 1 | 0.4514086 |
| X3 | 0.1937500 | 0.3535534 | -0.4992019 | 0.8867019 | 0.3003125 | 1 | 0.5836866 |
| X1*X3 | 0.1375000 | 0.5 | -0.8424820 | 1.1174820 | 0.0756250 | 1 | 0.7833162 |
| X1*X2 | -0.4125000 | 0.5 | -1.3924820 | 0.5674820 | 0.6806250 | 1 | 0.4093716 |
| X2*X3 | -0.0400000 | 0.5 | -1.0199820 | 0.9399820 | 0.0064000 | 1 | 0.9362373 |
| X1*X1 | 3.1825 | 0.5204165 | 2.1625024 | 4.2024976 | 37.3968231 | 1 | 0E-7 |
| X2*X2 | 0.2700000 | 0.5204165 | -0.7499976 | 1.2899976 | 0.2691692 | 1 | 0.6038896 |
| X3*X3 | -0.1800000 | 0.5204165 | -1.1999976 | 0.8399976 | 0.1196308 | 1 | 0.7294353 |

Results, k5:

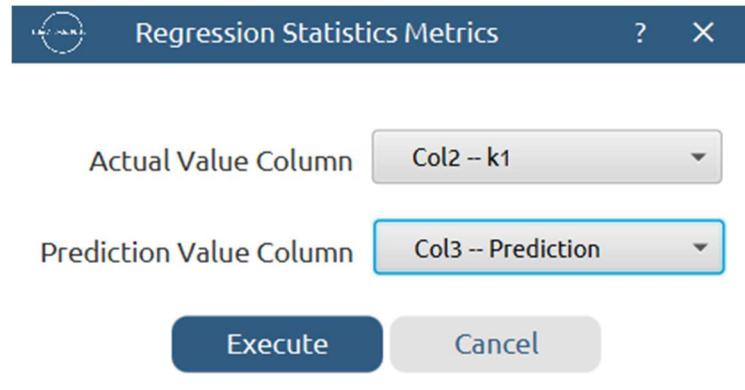
| k5 | Prediction |
|-------|------------|
| 1.39 | 1.4212500 |
| 15.31 | 14.8112500 |
| 1.29 | 1.7887500 |
| 13.13 | 13.0987500 |
| 1.2 | 0.9962500 |
| 12.51 | 12.8362500 |
| 1.4 | 1.0737500 |
| 13.73 | 13.9337500 |
| 3.27 | 3.4425000 |
| 3.17 | 2.875 |
| 3.84 | 4.1350000 |
| 3.53 | 3.3575000 |
| 3.34 | 3.2900000 |
| 3.35 | 3.2900000 |
| 3.18 | 3.2900000 |

| Goodness of Fit | |
|--------------------------------------|-------------|
| Value | |
| Deviance | 1.0471250 |
| Scaled Deviance | 1.0471250 |
| Pearson Chi-Square | 1.0471250 |
| Scaled Pearson Chi-Square | 1.0471250 |
| Log Likelihood | -14.3076405 |
| Akaike's Information Criterion (AIC) | 48.6152810 |
| Finite Sample Corrected AIC (AICC) | 103.6152810 |
| Bayesian Information Criterion (BIC) | 55.6957830 |
| Consistent AIC (CAIC) | 65.6957830 |

| Parameter Estimates | | | | | | | |
|---------------------|-------------|------------|------------|-----------|----------------|----|-----------|
| Variable | Coefficient | Std. Error | Lower CI | Upper CI | Test Statistic | df | p-value |
| intercept | 3.2900000 | 0.5773503 | 2.1584143 | 4.4215857 | 32.4723000 | 1 | 0E-7 |
| X1 | 6.1750000 | 0.3535534 | 5.4820481 | 6.8679519 | 305.0450000 | 1 | 0.0 |
| X2 | -0.3362500 | 0.3535534 | -1.0292019 | 0.3567019 | 0.9045125 | 1 | 0.3415746 |
| X3 | 0.2937500 | 0.3535534 | -0.3992019 | 0.9867019 | 0.6903125 | 1 | 0.4060581 |
| X1*X3 | 0.2550000 | 0.5 | -0.7249820 | 1.2349820 | 0.2601000 | 1 | 0.6100515 |
| X1*X2 | -0.5200000 | 0.5 | -1.4999820 | 0.4599820 | 1.0816000 | 1 | 0.2983399 |
| X2*X3 | -0.0525000 | 0.5 | -1.0324820 | 0.9274820 | 0.0110250 | 1 | 0.9163758 |
| X1*X1 | 4.1237500 | 0.5204165 | 3.1037524 | 5.1437476 | 62.7888519 | 1 | 0E-7 |
| X2*X2 | 0.3662500 | 0.5204165 | -0.6537476 | 1.3862476 | 0.4952827 | 1 | 0.4815802 |
| X3*X3 | -0.2037500 | 0.5204165 | -1.2237476 | 0.8162476 | 0.1532827 | 1 | 0.6954178 |

Step 6: Regression Metrics

Create a tab named “Metrics – k1” and import the results from the spreadsheet “Regression – k1”. Then, produce the regression metrics for the k₁ regression equation: Statistics → Model Metrics → Regression Metrics



Results:

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) |
|-------------|-------------|--------------------|-------------------------|---------------------|-----------|
| User Header | User Row ID | Mean Squared Error | Root Mean Squared Error | Mean Absolute Error | R Squared |
| 1 | | 0.0003217 | 0.0179351 | 0.0153333 | 0.9986202 |

Repeat this step for the rest of the response variables. Results, k₂:

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) |
|-------------|-------------|--------------------|-------------------------|---------------------|-----------|
| User Header | User Row ID | Mean Squared Error | Root Mean Squared Error | Mean Absolute Error | R Squared |
| 1 | | 0.0022528 | 0.0474634 | 0.0385556 | 0.9978101 |

Results, k₃:

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) |
|-------------|-------------|--------------------|-------------------------|---------------------|-----------|
| User Header | User Row ID | Mean Squared Error | Root Mean Squared Error | Mean Absolute Error | R Squared |
| 1 | | 0.0073744 | 0.0858746 | 0.0682222 | 0.9980739 |

Results, k₄:

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) |
|-------------|-------------|--------------------|-------------------------|---------------------|-----------|
| User Header | User Row ID | Mean Squared Error | Root Mean Squared Error | Mean Absolute Error | R Squared |
| 1 | | 0.0423350 | 0.2057547 | 0.1630000 | 0.9972141 |

Results, k₅:

| | Col1 | Col2 (D) | Col3 (D) | Col4 (D) | Col5 (D) |
|-------------|-------------|--------------------|-------------------------|---------------------|-----------|
| User Header | User Row ID | Mean Squared Error | Root Mean Squared Error | Mean Absolute Error | R Squared |
| 1 | | 0.0698083 | 0.2642127 | 0.2183333 | 0.9971917 |

Step 7: Analysis of Covariance

Create a new tab named “ANCOVA – k1” and import the results from the spreadsheet “Normalized data”. Afterwards perform analysis of covariance for k₁: Statistics → Analysis of (Co)Variance → ANCOVA

ANCOVA
?
X

Confidence Level (%)

Dependent Variable

Sum of Squares For Tests

Coding for Factors

Excluded Columns

Factors

Covariates

Custom
 Include All Main Effects
 Full Factorial

X1+X2+X3+X1:X1+X2:X2+X3:X3+X1:X2+X2:X3+X1:X3
Execute
Cancel

Results:

| | Col1 | Col2 (S) | Col3 (I) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) |
|-------------|-------------|----------|----------|-----------|-----------|--------------|-----------|
| User Header | User Row ID | Source | DF | Adj SS | Adj MS | F-Value | P-Value |
| 1 | | X1 | 1 | 3.0752000 | 3.0752000 | 3186.7357513 | 0E-7 |
| 2 | | X2 | 1 | 0.0036125 | 0.0036125 | 3.7435233 | 0.1108040 |
| 3 | | X3 | 1 | 0.0078125 | 0.0078125 | 8.0958549 | 0.0360208 |
| 4 | | X1*X1 | 1 | 0.3930058 | 0.3930058 | 407.2598645 | 0.0000055 |
| 5 | | X2*X2 | 1 | 0.0020827 | 0.0020827 | 2.1582304 | 0.2017501 |
| 6 | | X3*X3 | 1 | 0.0009750 | 0.0009750 | 1.0103627 | 0.3609527 |
| 7 | | X1*X2 | 1 | 0.0049000 | 0.0049000 | 5.0777202 | 0.0739628 |
| 8 | | X2*X3 | 1 | 0.0002250 | 0.0002250 | 0.2331606 | 0.6495899 |
| 9 | | X1*X3 | 1 | 0.0009000 | 0.0009000 | 0.9326425 | 0.3785314 |
| 10 | | Error | 5 | 0.0048250 | 0.0009650 | | |
| 11 | | Total | 14 | 3.4968400 | | | |

Repeat this step for the rest of the response variables. Results, k_2 :

| | Col1 | Col2 (S) | Col3 (I) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) |
|-------------|-------------|----------|----------|------------|------------|--------------|-----------|
| User Header | User Row ID | Source | DF | Adj SS | Adj MS | F-Value | P-Value |
| 1 | | X1 | 1 | 13.2612500 | 13.2612500 | 1962.2071517 | 1E-7 |
| 2 | | X2 | 1 | 0.0406125 | 0.0406125 | 6.0092478 | 0.0578384 |
| 3 | | X3 | 1 | 0.0136125 | 0.0136125 | 2.0141800 | 0.2150568 |
| 4 | | X1*X1 | 1 | 2.0037333 | 2.0037333 | 296.4833539 | 0.0000121 |
| 5 | | X2*X2 | 1 | 0.0231410 | 0.0231410 | 3.4240728 | 0.1234812 |
| 6 | | X3*X3 | 1 | 0.0061564 | 0.0061564 | 0.9109362 | 0.3836976 |
| 7 | | X1*X2 | 1 | 0.0380250 | 0.0380250 | 5.6263872 | 0.0637942 |
| 8 | | X2*X3 | 1 | 0.0004000 | 0.0004000 | 0.0591862 | 0.8174527 |
| 9 | | X1*X3 | 1 | 0.0006250 | 0.0006250 | 0.0924784 | 0.7732987 |
| 10 | | Error | 5 | 0.0337917 | 0.0067583 | | |
| 11 | | Total | 14 | 15.4306 | | | |

Results, k₃:

| | Col1 | Col2 (S) | Col3 (I) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) |
|-------------|-------------|----------|----------|------------|------------|--------------|-----------|
| User Header | User Row ID | Source | DF | Adj SS | Adj MS | F-Value | P-Value |
| 1 | | X1 | 1 | 48.5112500 | 48.5112500 | 2192.7640500 | 1E-7 |
| 2 | | X2 | 1 | 0.1200500 | 0.1200500 | 5.4263975 | 0.0672562 |
| 3 | | X3 | 1 | 0.1104500 | 0.1104500 | 4.9924665 | 0.0757469 |
| 4 | | X1*X1 | 1 | 8.2892410 | 8.2892410 | 374.6831863 | 0.0000068 |
| 5 | | X2*X2 | 1 | 0.0561641 | 0.0561641 | 2.5386817 | 0.1719677 |
| 6 | | X3*X3 | 1 | 0.0217026 | 0.0217026 | 0.9809807 | 0.3674357 |
| 7 | | X1*X2 | 1 | 0.1225000 | 0.1225000 | 5.5371403 | 0.0653071 |
| 8 | | X2*X3 | 1 | 0.0016000 | 0.0016000 | 0.0723218 | 0.7987297 |
| 9 | | X1*X3 | 1 | 0.0256000 | 0.0256000 | 1.1571493 | 0.3312016 |
| 10 | | Error | 5 | 0.1106167 | 0.0221233 | | |
| 11 | | Total | 14 | 57.4298933 | | | |

Results, k₄:

| | Col1 | Col2 (S) | Col3 (I) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) |
|-------------|-------------|----------|----------|-------------|-------------|--------------|-----------|
| User Header | User Row ID | Source | DF | Adj SS | Adj MS | F-Value | P-Value |
| 1 | | X1 | 1 | 187.5984500 | 187.5984500 | 1477.0949963 | 2E-7 |
| 2 | | X2 | 1 | 0.5671125 | 0.5671125 | 4.4652770 | 0.0882720 |
| 3 | | X3 | 1 | 0.3003125 | 0.3003125 | 2.3645723 | 0.1847281 |
| 4 | | X1*X1 | 1 | 37.3968231 | 37.3968231 | 294.4515813 | 0.0000123 |
| 5 | | X2*X2 | 1 | 0.2691692 | 0.2691692 | 2.1193593 | 0.2052169 |
| 6 | | X3*X3 | 1 | 0.1196308 | 0.1196308 | 0.9419375 | 0.3763547 |
| 7 | | X1*X2 | 1 | 0.6806250 | 0.6806250 | 5.3590410 | 0.0684824 |
| 8 | | X2*X3 | 1 | 0.0064000 | 0.0064000 | 0.0503917 | 0.8312681 |
| 9 | | X1*X3 | 1 | 0.0756250 | 0.0756250 | 0.5954490 | 0.4751894 |
| 10 | | Error | 5 | 0.6350250 | 0.1270050 | | |
| 11 | | Total | 14 | 227.9421733 | | | |

Results, k₅:

| | Col1 | Col2 (S) | Col3 (I) | Col4 (D) | Col5 (D) | Col6 (D) | Col7 (D) |
|-------------|-------------|----------|----------|-------------|-------------|--------------|-----------|
| User Header | User Row ID | Source | DF | Adj SS | Adj MS | F-Value | P-Value |
| 1 | | X1 | 1 | 305.0450000 | 305.0450000 | 1456.5835024 | 2E-7 |
| 2 | | X2 | 1 | 0.9045125 | 0.9045125 | 4.3190283 | 0.0922696 |
| 3 | | X3 | 1 | 0.6903125 | 0.6903125 | 3.2962278 | 0.1291463 |
| 4 | | X1*X1 | 1 | 62.7888519 | 62.7888519 | 299.8154562 | 0.0000118 |
| 5 | | X2*X2 | 1 | 0.4952827 | 0.4952827 | 2.3649645 | 0.1846978 |
| 6 | | X3*X3 | 1 | 0.1532827 | 0.1532827 | 0.7319217 | 0.4313380 |
| 7 | | X1*X2 | 1 | 1.0816000 | 1.0816000 | 5.1646174 | 0.0722053 |
| 8 | | X2*X3 | 1 | 0.0110250 | 0.0110250 | 0.0526441 | 0.8276149 |
| 9 | | X1*X3 | 1 | 0.2601000 | 0.2601000 | 1.2419721 | 0.3157732 |
| 10 | | Error | 5 | 1.0471250 | 0.2094250 | | |
| 11 | | Total | 14 | 372.8643600 | | | |

References

(1) Jovanović, M.; Rakić, T.; Tumpa, A.; Jančić Stojanović, B. Quality by Design Approach in the Development of Hydrophilic Interaction Liquid Chromatographic Method for the Analysis of Iohexol and Its Impurities. *Journal of Pharmaceutical and Biomedical Analysis* 2015, 110, 42–48. <https://doi.org/10.1016/j.jpba.2015.02.046>.